## Binary Conversions

## Corresponding Material

Number Systems

## Discussion

There are a lot of different number systems that are used in computer science. There have also been different number systems used in the past such as the Maya Number System and the Babylonian Number System. All number systems have a base. The most common is the decimal system with base ten. Two other systems that are used by computers are the binary system with base two and the hexadecimal system with base sixteen.

## Binary to Decimal

## Example:

| Binary | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Base | $2^{7}$ | $2^{6}$ | $2^{5}$ | $2^{4}$ | $2^{3}$ | $2^{2}$ | $2^{1}$ | $2^{0}$ |
| Math | $1 \times 128$ | $0 \times 64$ | $0 \times 32$ | $1 \times 16$ | $1 \times 8$ | $0 \times 4$ | $0 \times 2$ | $1 \times 1$ |
| Decimal | $\mathbf{1 2 8}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1 6}$ | $\mathbf{8}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ |

Answer: 128 + $16+8+1=153$

## Exercise:

| Binary | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Base | $2^{7}$ | $2^{6}$ | $2^{5}$ | $2^{4}$ | $2^{3}$ | $2^{2}$ | $2^{1}$ | $2^{0}$ |
| Math |  |  |  |  |  |  |  |  |
| Decimal |  |  |  |  |  |  |  |  |

Answer:

## CodeHS

Decimal to Binary

## Example:

Starting Number: 172

| Decimal | $\mathbf{1 7 2}$ | $\mathbf{4 4}$ | $\mathbf{4 4}$ | $\mathbf{1 2}$ | $\mathbf{1 2}$ | $\mathbf{4}$ | $\mathbf{0}$ | $\mathbf{0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Base | $2^{7}$ | $2^{6}$ | $2^{5}$ | $2^{4}$ | $2^{3}$ | $2^{2}$ | $2^{1}$ | $2^{0}$ |
| Math | $172 \div 128$ | $44 \div 64$ | $44 \div 32$ | $12 \div 16$ | $12 \div 8$ | $4 \div 4$ | $0 \div 2$ | $0 \div 1$ |
| Divides? | $172-128$ <br> $=\mathbf{4 4}$ | $\mathbf{4 4}$ | $44-32$ <br> $=12$ | $\mathbf{1 2}$ | $12-8=$ <br> $\mathbf{4}$ | $4-4=$ <br> $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ |
| Binary | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{0}$ |

Answer: 10101100

## Exercise:

Starting Number: 210

| Decimal | 210 | 82 | 18 | 18 | 2 | 2 | 2 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Base | $2^{7}$ | $2^{6}$ | $2^{5}$ | $2^{4}$ | $2^{3}$ | $2^{2}$ | $2^{1}$ | $2^{0}$ |
| Math |  |  |  |  |  |  |  |  |
| Divides? |  |  |  |  |  |  |  |  |
| Binary |  |  |  |  |  |  |  |  |

Answer:

Further Practice:

| Decimal | Binary |
| :---: | :---: |
| 250 |  |
|  | 10101010 |
| 87 | 01111100 |
| 99 |  |

